

EE 230

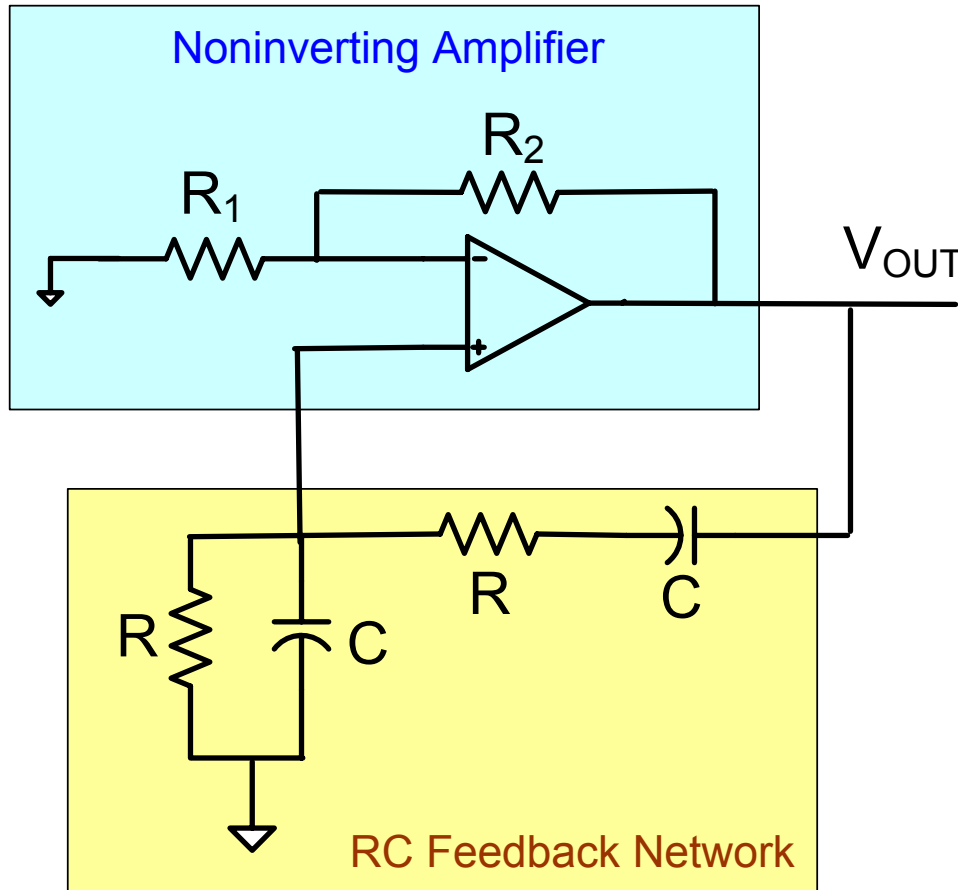
Lecture 29

Nonlinear Circuits and Nonlinear Devices

- Diode
- BJT
- MOSFET

Review from Last Time:

Wein-Bridge Oscillator



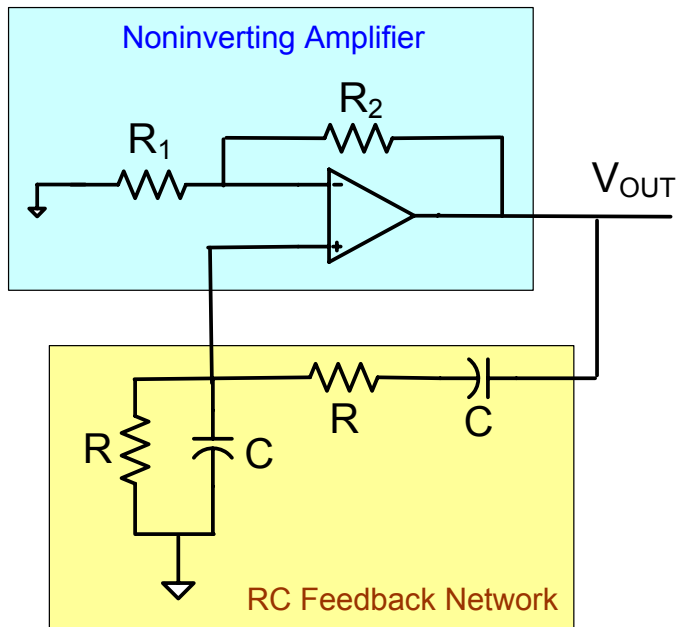
$$K_o = 1 + \frac{R_2}{R_1} = 3 + \varepsilon$$

$$\omega_{osc} \approx \frac{1}{RC}$$

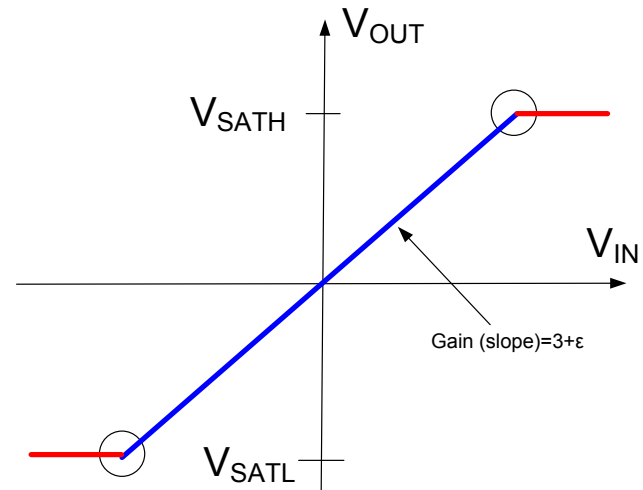
Nonlinearity of Noninverting Amplifier Limits Amplitude of V_{OUT} and when saturation occurs, will cause distortion

Review from Last Time:

Wein-Bridge Oscillator



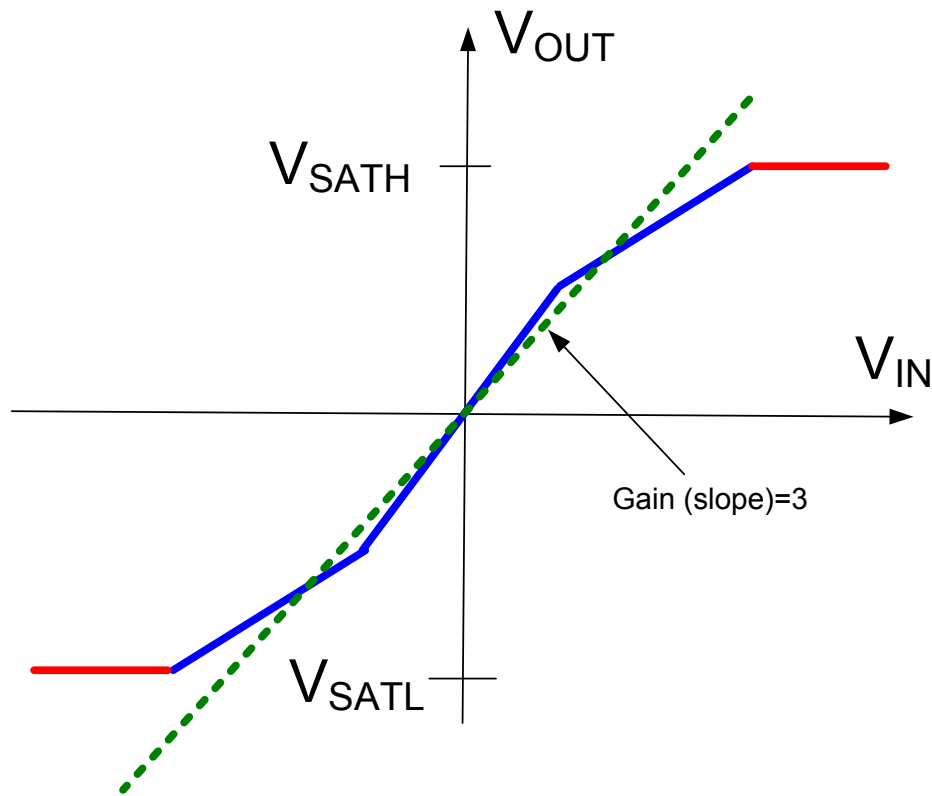
$$K_o = 1 + \frac{R_2}{R_1} = 3 + \epsilon$$



Nonlinearity of Noninverting Amplifier

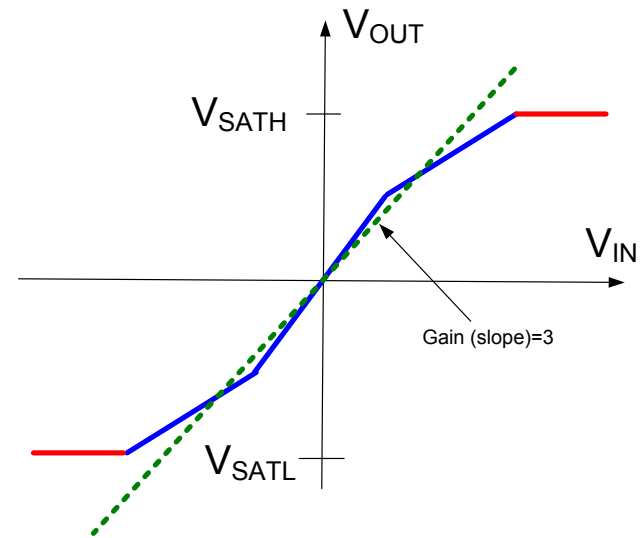
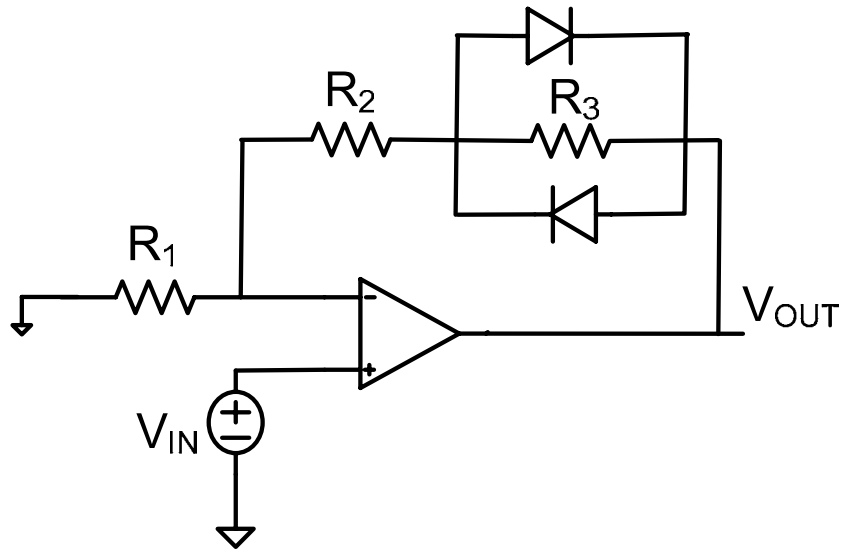
Review from Last Time:

Amplifiers with less abrupt change in slope will reduce distortion



Review from Last Time:

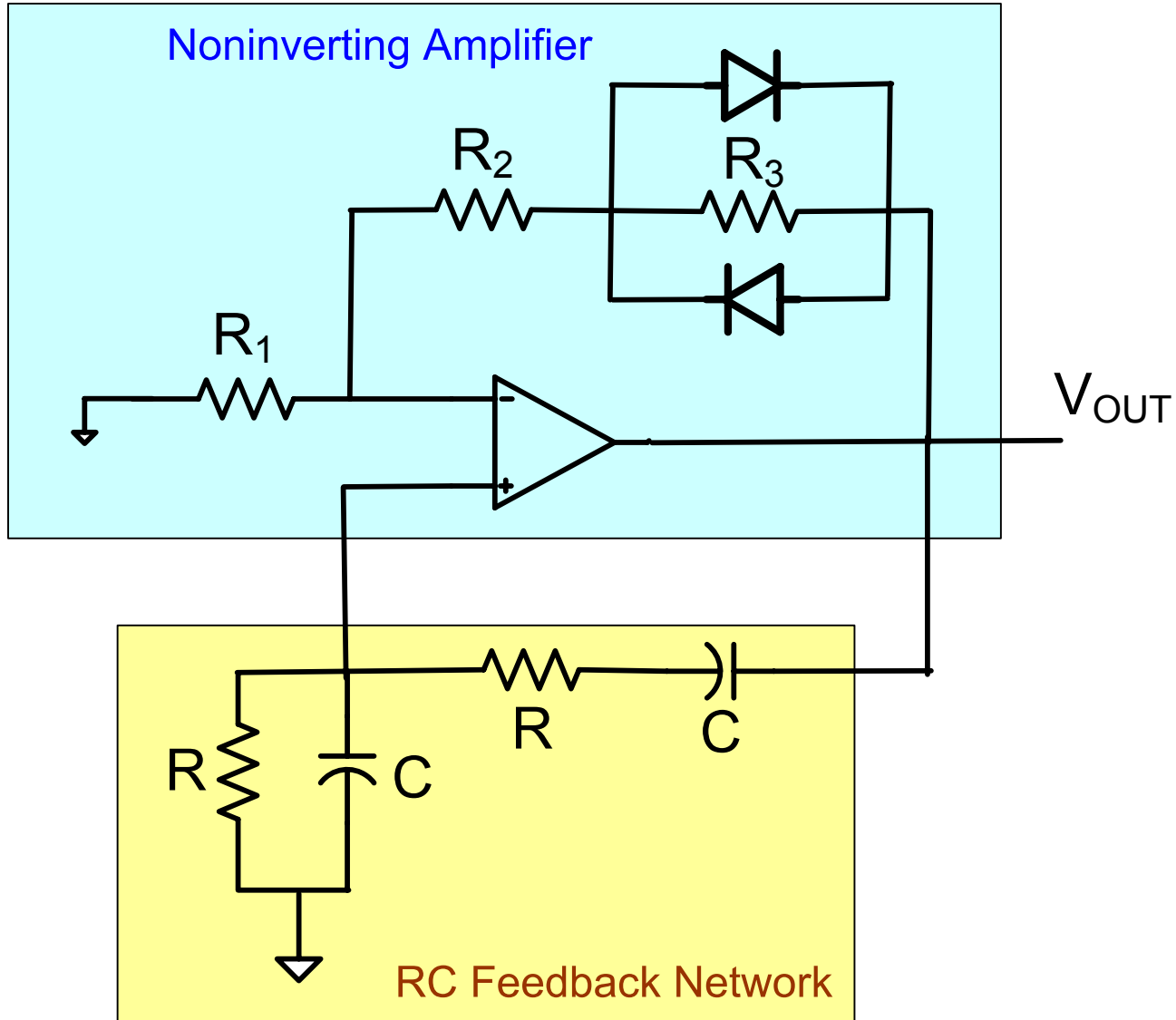
Amplifiers with less abrupt change in slope



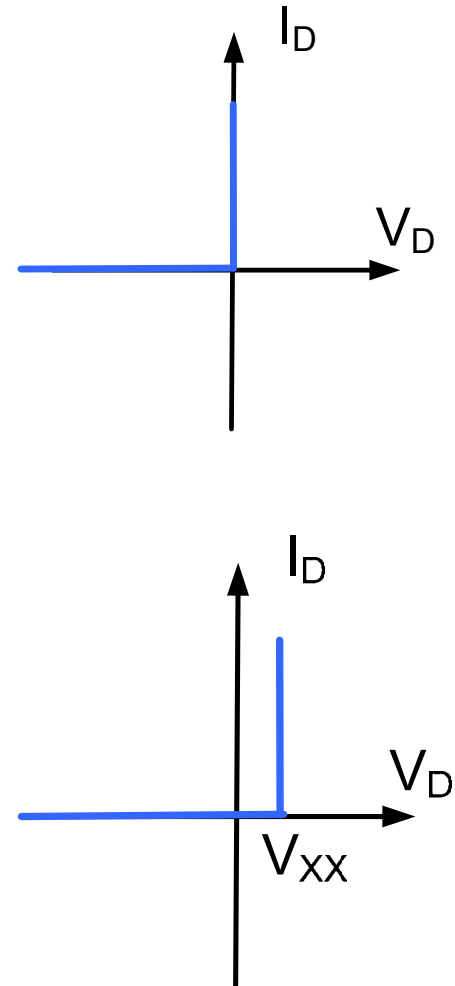
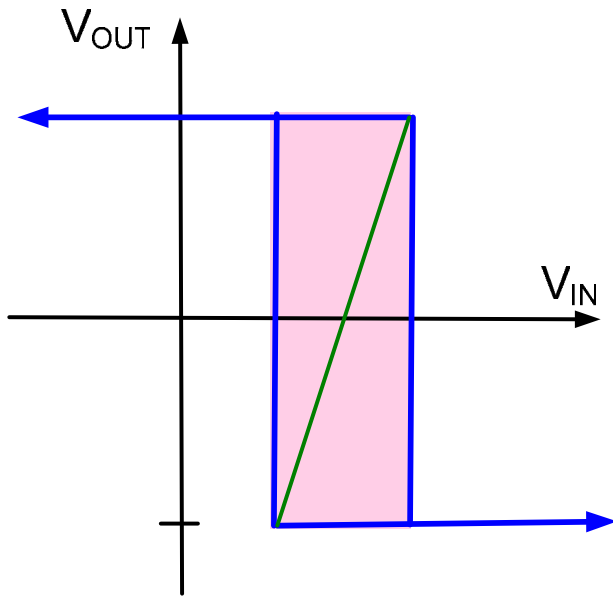
$$V_{OUT} = \begin{cases} \left(1 + \frac{R_2}{R_1}\right) V_{IN} + V_Y & V_{IN} \geq \frac{R_1}{R_3} V_Y \\ \left(1 + \frac{R_2}{R_1}\right) V_{IN} & -\frac{R_1}{R_3} V_Y < V_{IN} < \frac{R_1}{R_3} V_Y \\ \left(1 + \frac{R_2}{R_1}\right) V_{IN} - V_Y & V_{IN} \leq -\frac{R_1}{R_3} V_Y \end{cases}$$

Review from Last Time:

Wein-Bridge Oscillator with Low Distortion Amplitude Limiting



Observation: Nonlinear Devices Have Provided Very Useful Performance Capabilities Not Obtainable with Linear Circuits



The Electronics World as We See It Until Now

Linear Circuits

Resistive Networks

Amplifiers
(Dependent Sources)

Passive Filters
(RLC Networks)

Active Filters

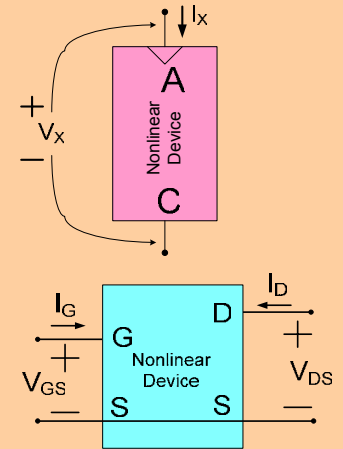
Waveform Generators

Sensor Interfaces

Analog to Digital Converters (ADC)

Digital to Analog Converters (DAC)

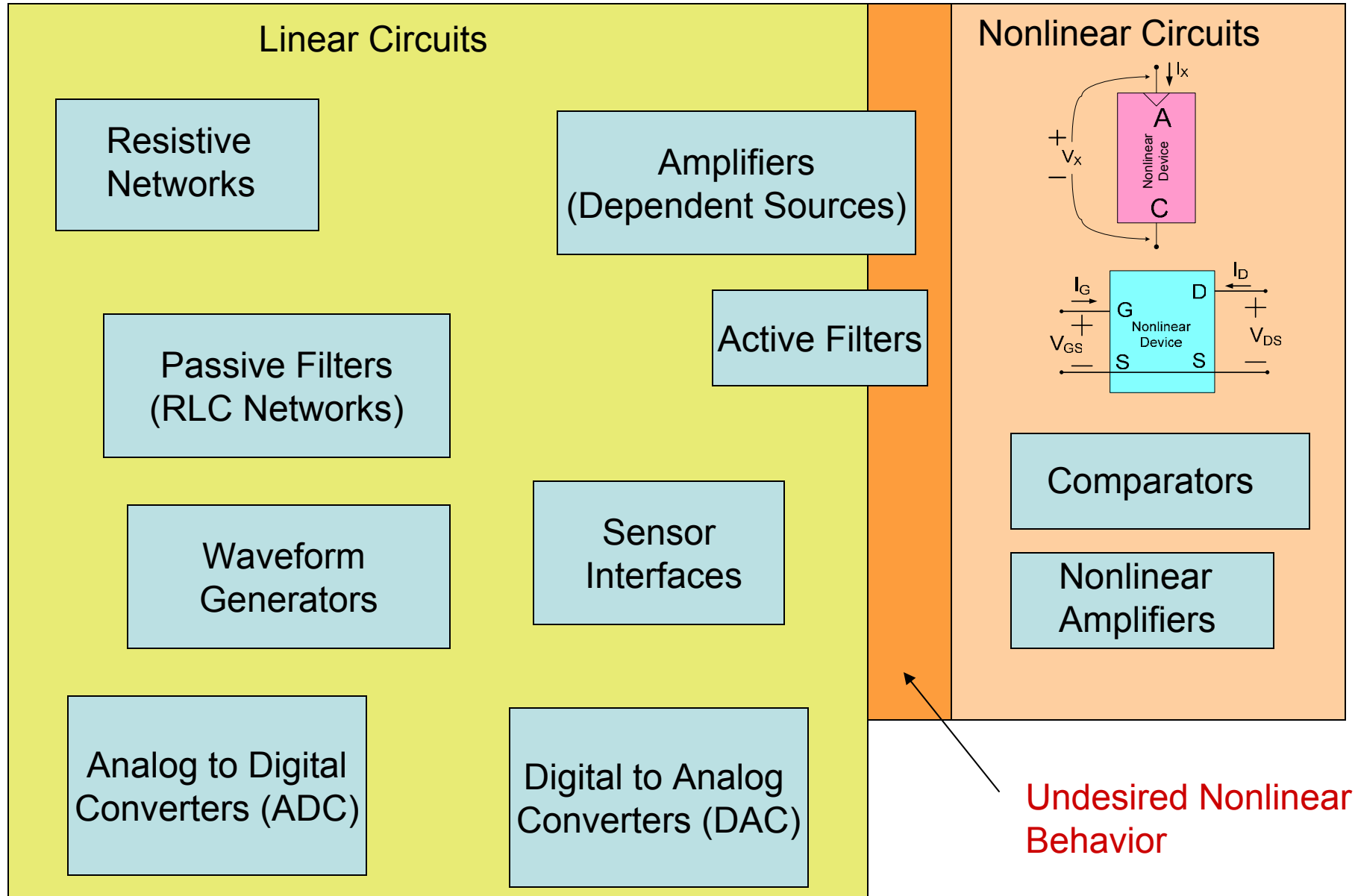
Nonlinear Circuits



Comparators

Nonlinear Amplifiers

The Electronics World as We See It Until Now



The Electronics World as We See It Until Now

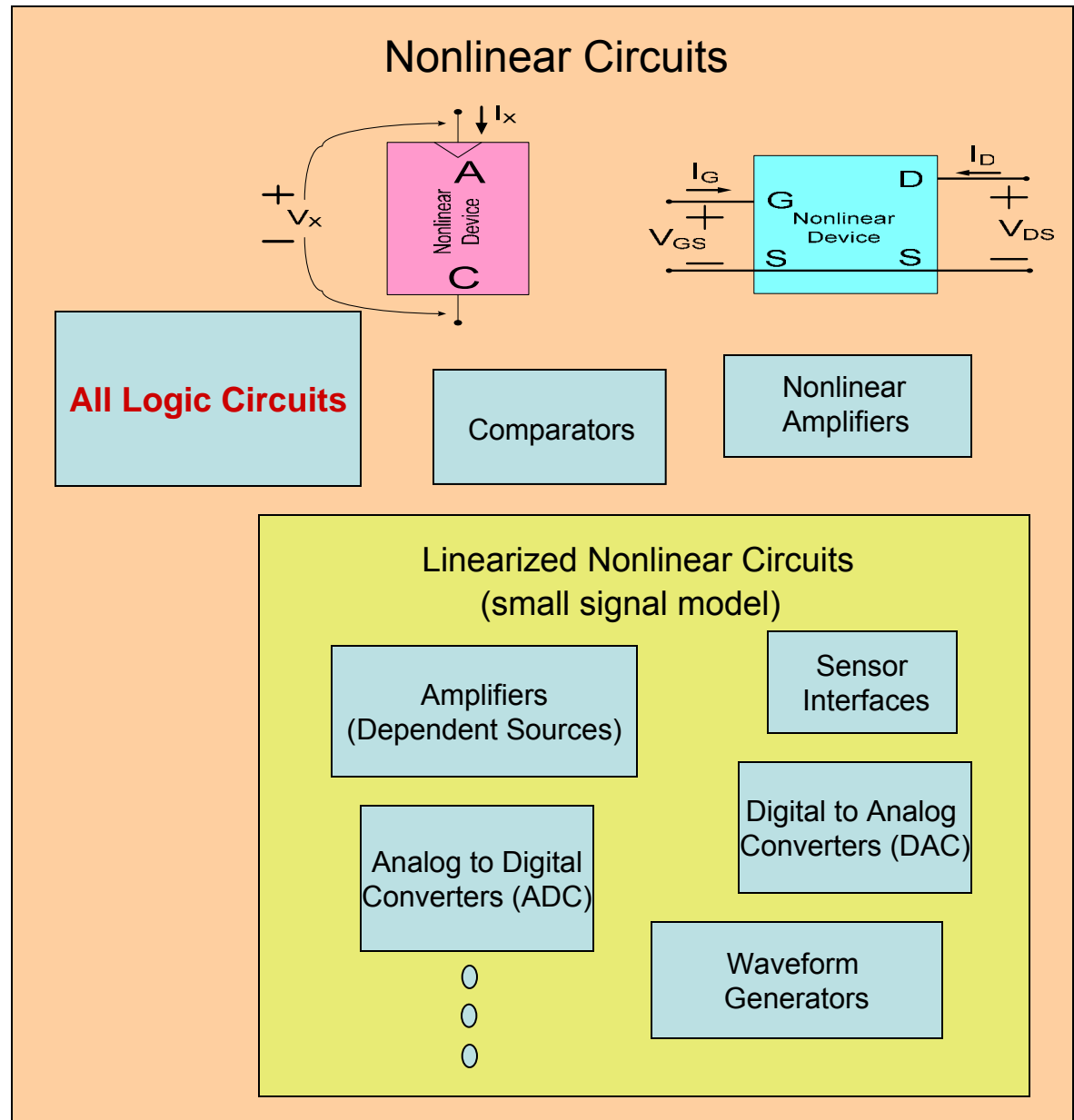
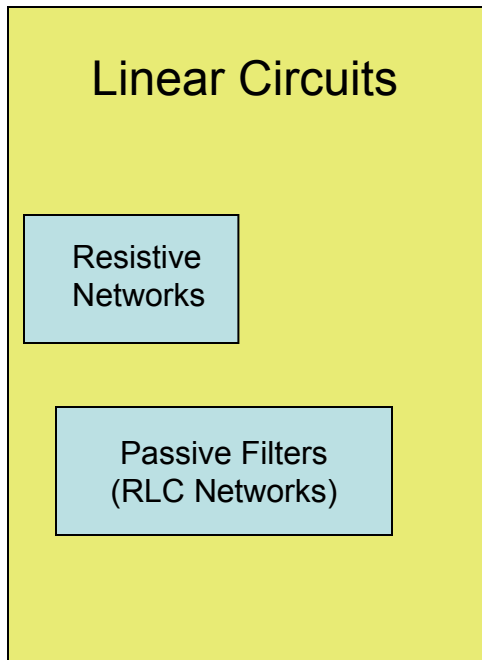
Perception:

Most of the Electronics World Is Linear

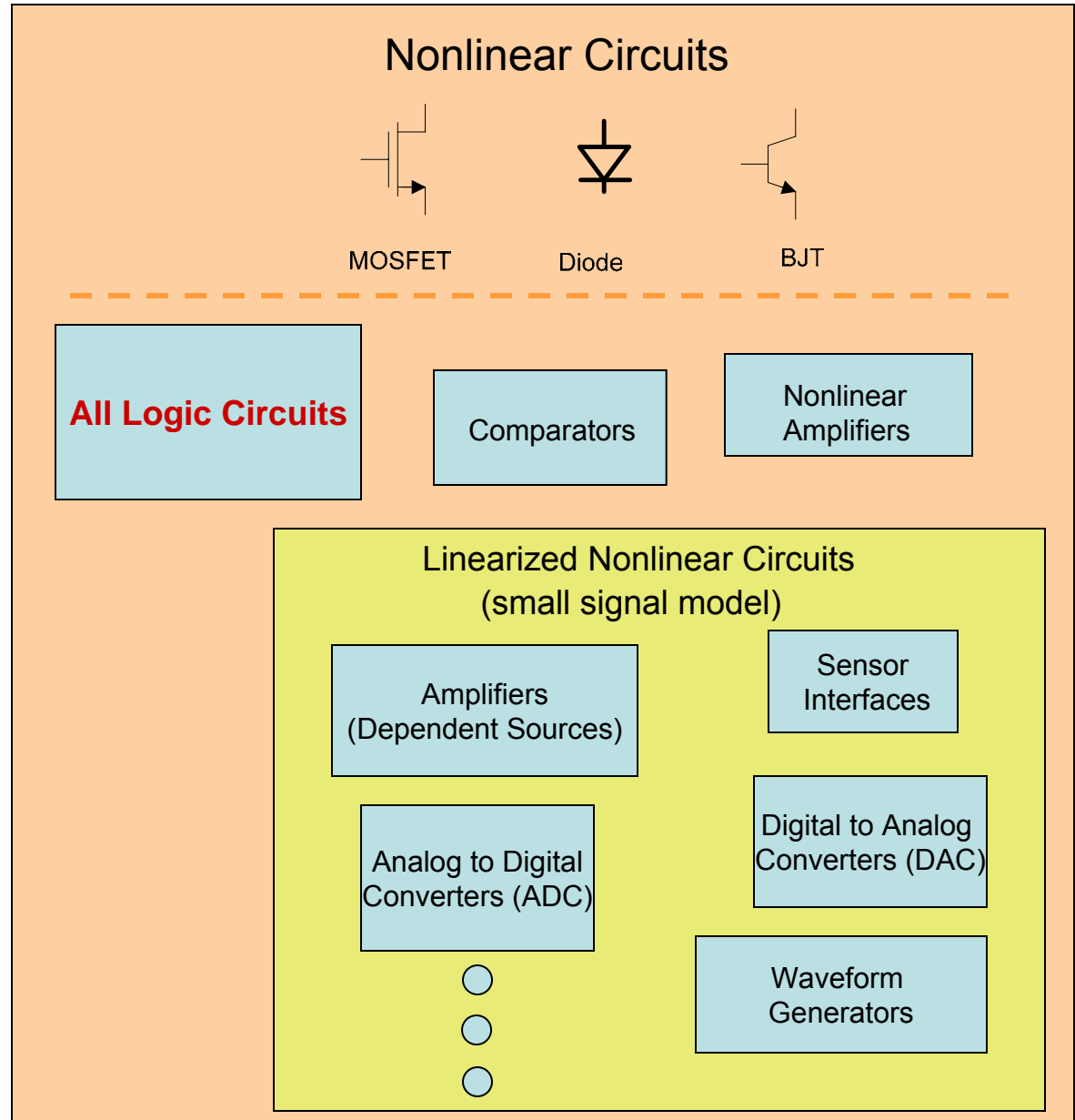
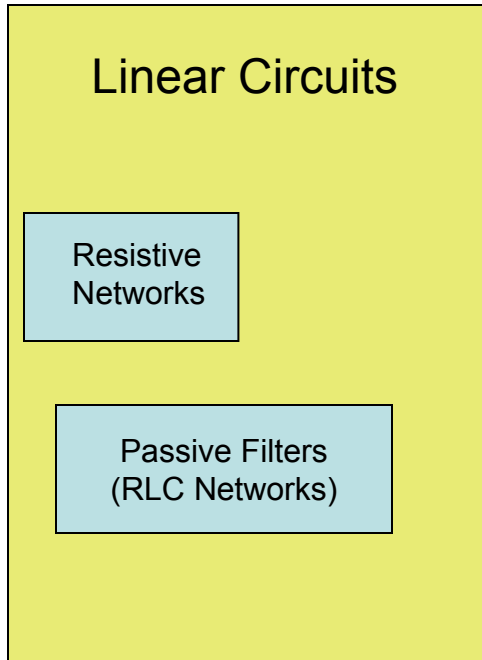
A few Useful Nonlinear Applications

Nonlinear Analysis is Hard

The Real Electronics World



The Real Electronics World



The Real Electronics World

Perception:

Most of the Electronics World Is Linear

A few Useful Nonlinear Applications

Nonlinear Analysis is Hard

Reality:

Most Electronic Circuits are Nonlinear

Many combine nonlinear devices to make nearly linear circuits

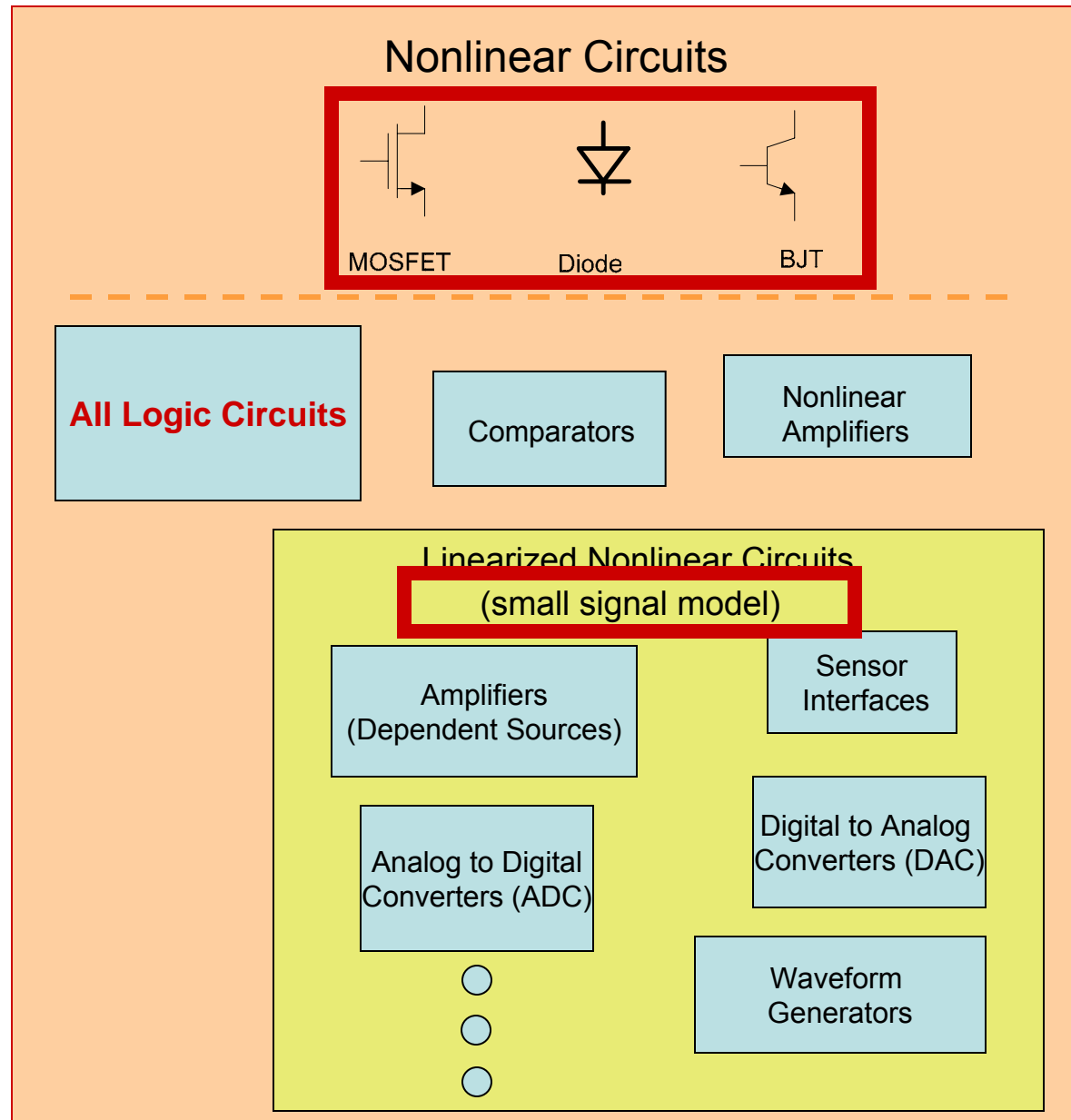
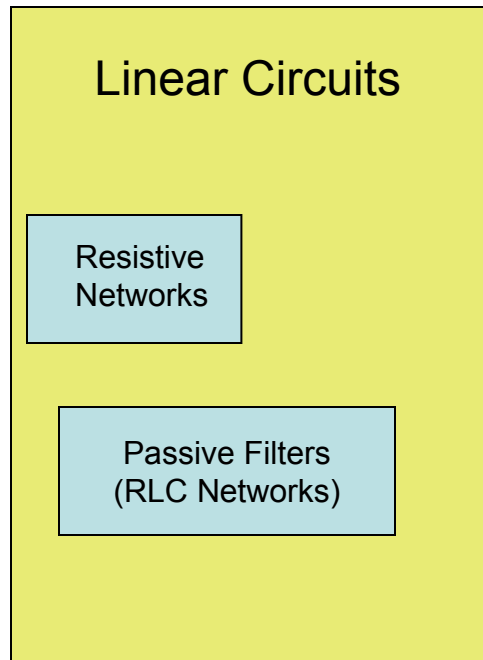
Nonlinear Analysis is Different

Sometimes Easier than Linear Analysis

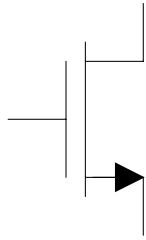
Sometimes Harder than Linear Analysis

But mostly just different

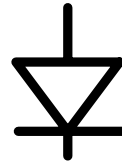
The Real Electronics World



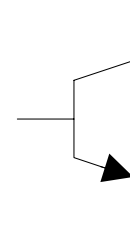
Basic Nonlinear Devices



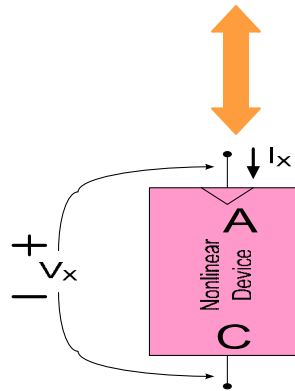
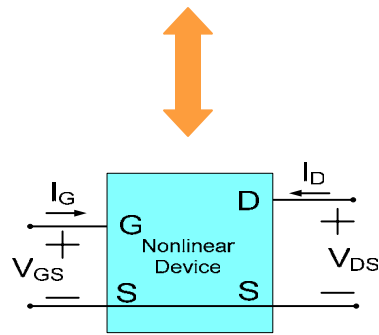
MOSFET



Diode



BJT



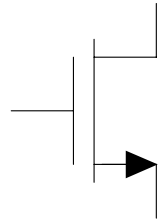
$$I_G = 0$$

$$I_D = \begin{cases} 0 & V_{GS} < 1V \\ 10^{-4} \left(V_{GS} - 1 - \frac{V_{DS}}{2} \right) V_{DS} & V_{GS} > 1V, V_{DS} < V_{GS} - 1V \\ \frac{10^{-4}}{2} (V_{GS} - 1)^2 & V_{GS} > 1V, V_{DS} > V_{GS} - 1V \end{cases}$$

$$I_D = 0 \quad \text{if} \quad V_D \leq 0$$

$$V_D = 0 \quad \text{if} \quad I_D > 0$$

Basic Nonlinear Devices



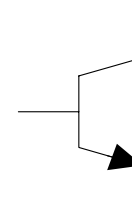
MOSFET

Proposed in approx 1930
Manufactured in approx 1970
Dominant device in digital ICs today
Widely used for analog ICs
Device upon which semiconductor industry today is based



Diode

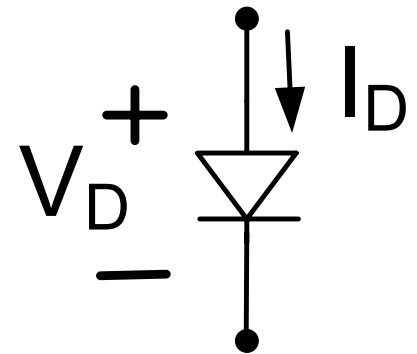
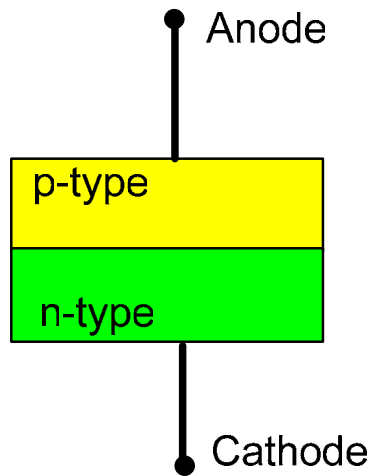
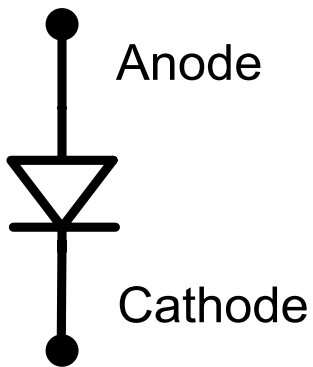
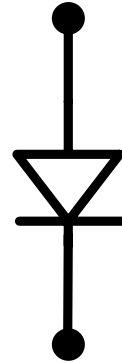
Proposed and manufactured in approx 1940
Physics understood approx 1948
Widely used in power applications
Some use in signal processing and instrumentation
Available in most semiconductor processes without additional cost but often not optimized



BJT

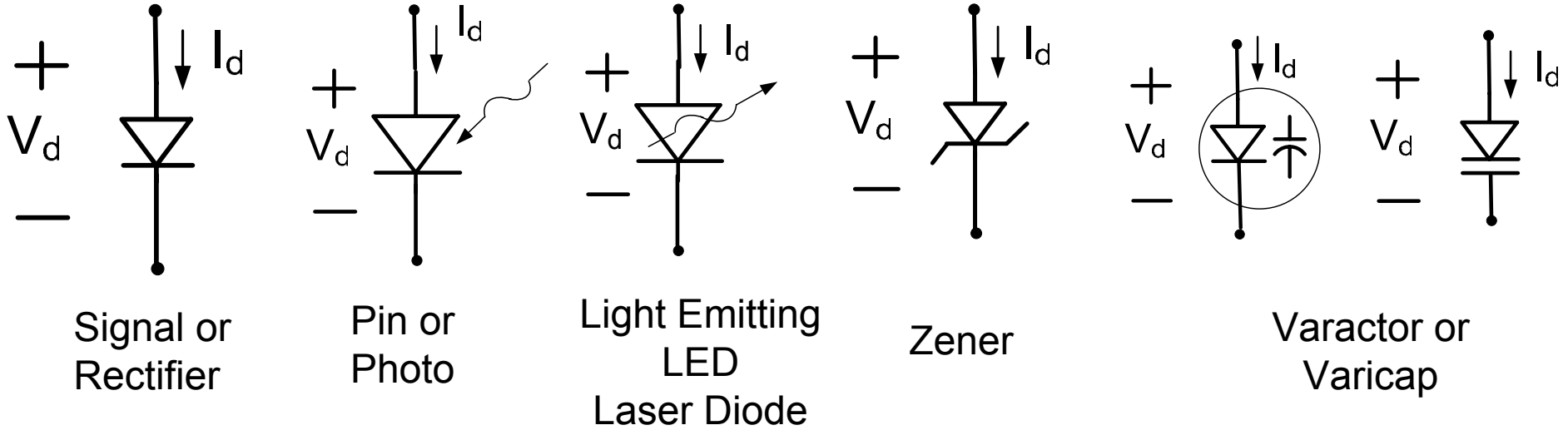
Invented in 1948 and manufactured almost immediately thereafter
Dominant device in semiconductor industry till mid 70s
Preferred in many linear ICs
Offers some speed benefits over MOSFET
Good BJTs available in some niche processes

The Diode

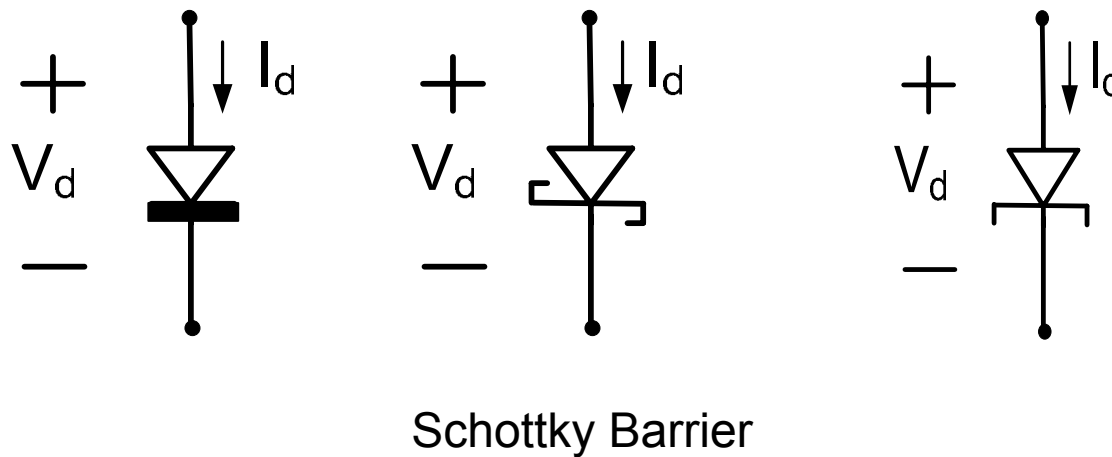


Types of Diodes

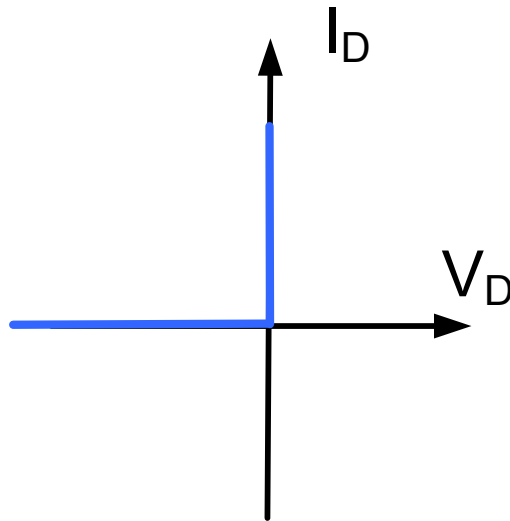
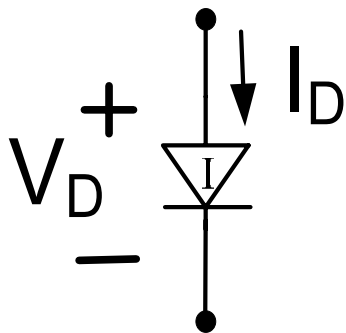
pn junction diodes



Metal-semiconductor junction diodes

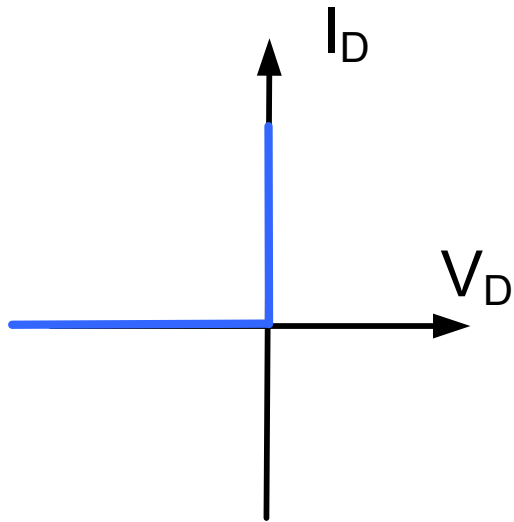


The Ideal Diode



$$I_D = 0 \quad \text{if} \quad V_D \leq 0$$
$$V_D = 0 \quad \text{if} \quad I_D > 0$$

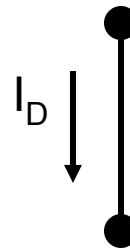
The Ideal Diode



$$I_D = 0 \quad \text{if} \quad V_D \leq 0 \quad \text{“OFF”}$$
$$V_D = 0 \quad \text{if} \quad I_D > 0 \quad \text{“ON”}$$

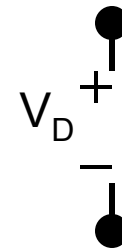


“ON”



$$I_D > 0$$

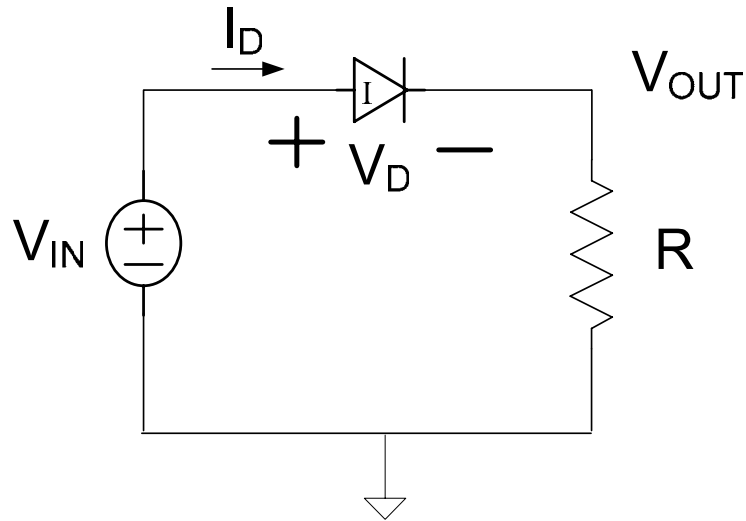
“OFF”



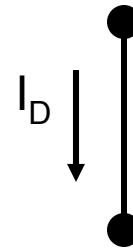
$$V_D \leq 0$$

Valid for

Consider a simple diode circuit

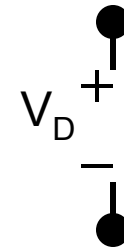


“ON”



$$I_D > 0$$

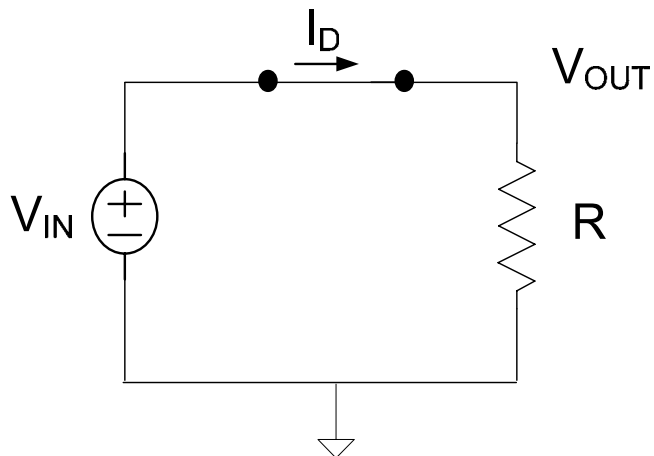
“OFF”



$$V_D \leq 0$$

Analysis:

Case 1 Guess Diode in “ON”



solution:

$$V_{OUT} = V_{IN}$$

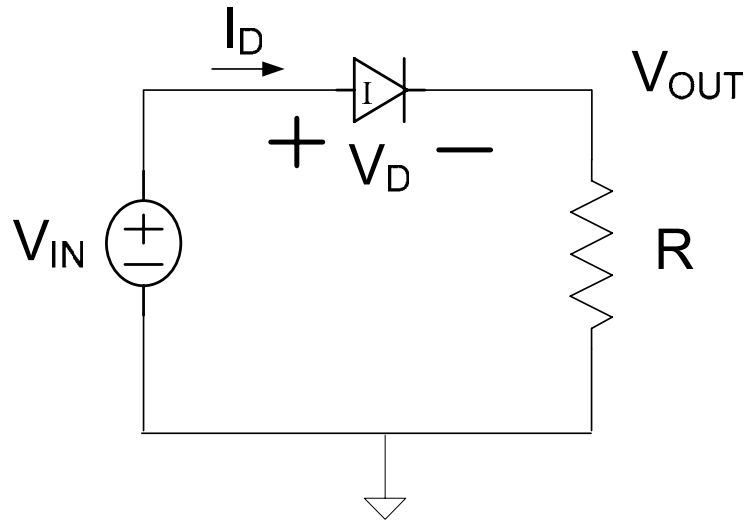
valid for:

$$I_D > 0$$

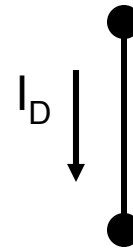
$$I_D = \frac{V_{OUT}}{R} \quad \text{Always express in terms of } V_{IN} \quad I_D = \frac{V_{IN}}{R}$$

$$V_{IN} > 0$$

Consider a simple diode circuit

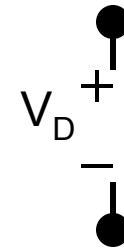


“ON”



$$I_D > 0$$

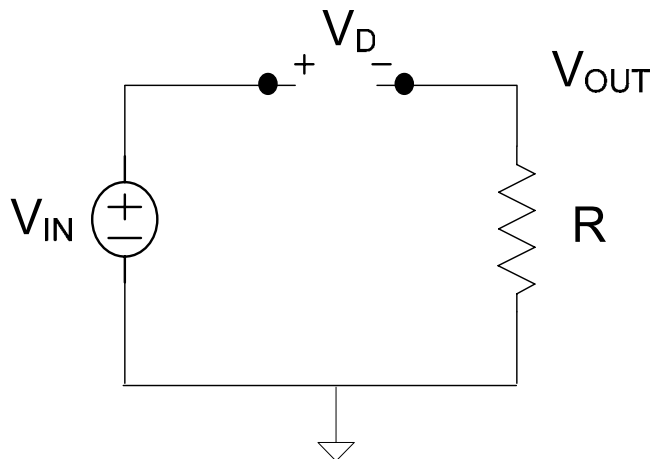
“OFF”



$$V_D \leq 0$$

Analysis:

Case 2 Guess Diode is “OFF”



solution:

$$V_{OUT} = 0$$

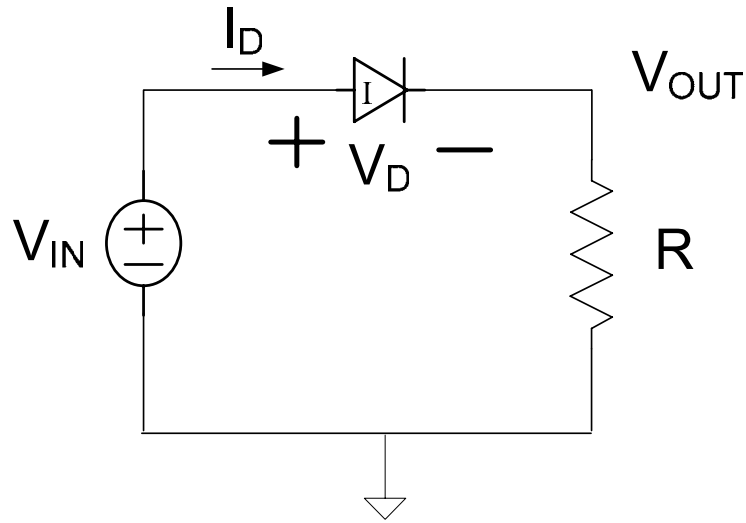
valid for:

$$V_D \leq 0$$

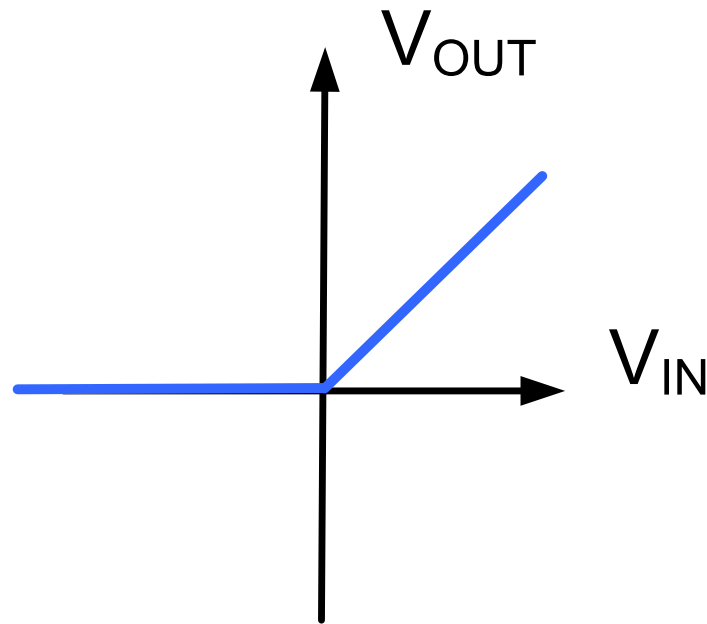
$$V_D = V_{IN} - V_{OUT} = V_{IN} \leq 0$$

$$V_{IN} \leq 0$$

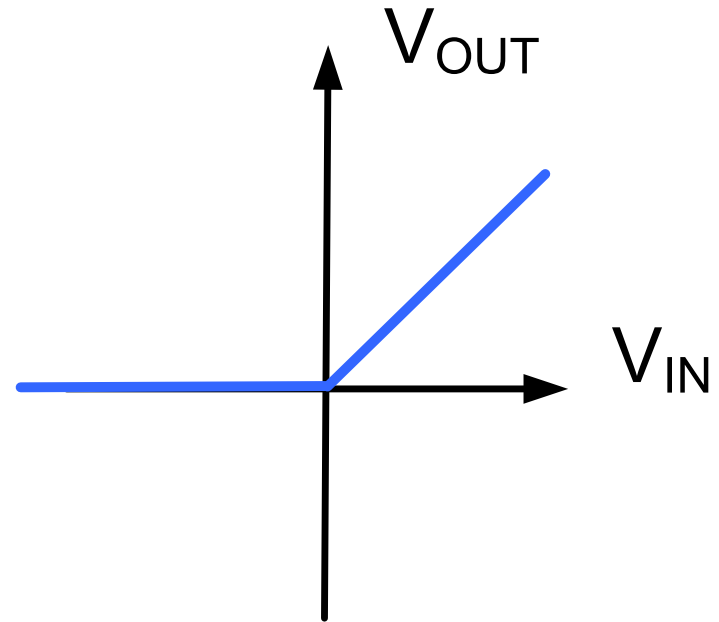
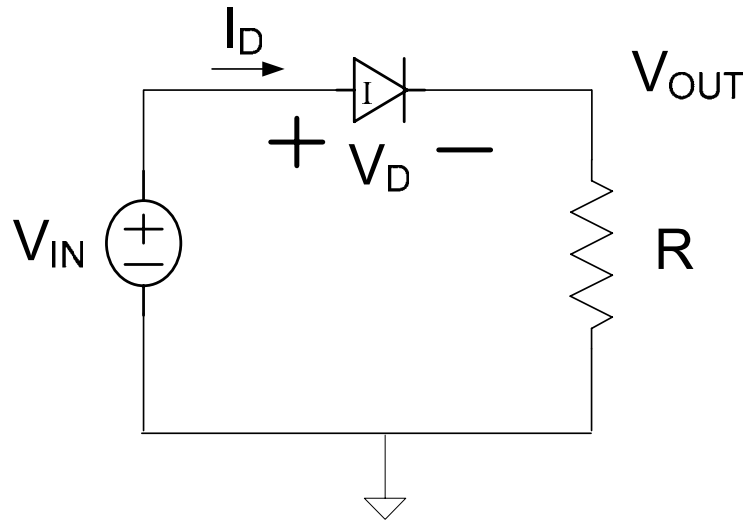
Consider a simple diode circuit



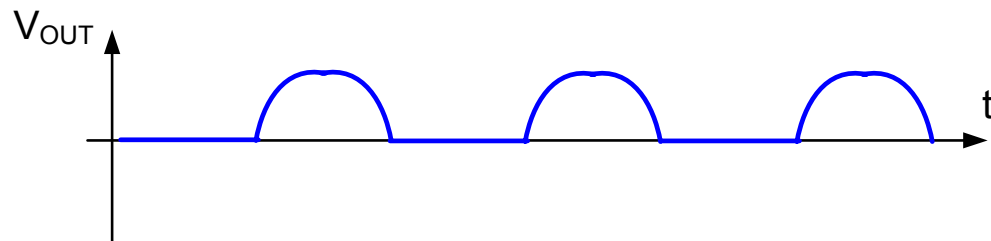
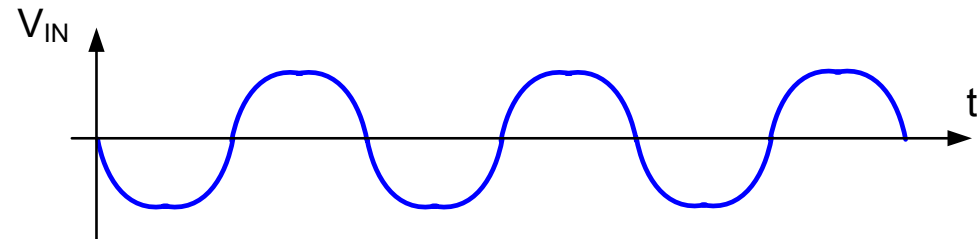
$$V_{OUT} = \begin{cases} V_{IN} & V_{IN} > 0 \\ 0 & V_{IN} \leq 0 \end{cases}$$



Consider a simple diode circuit



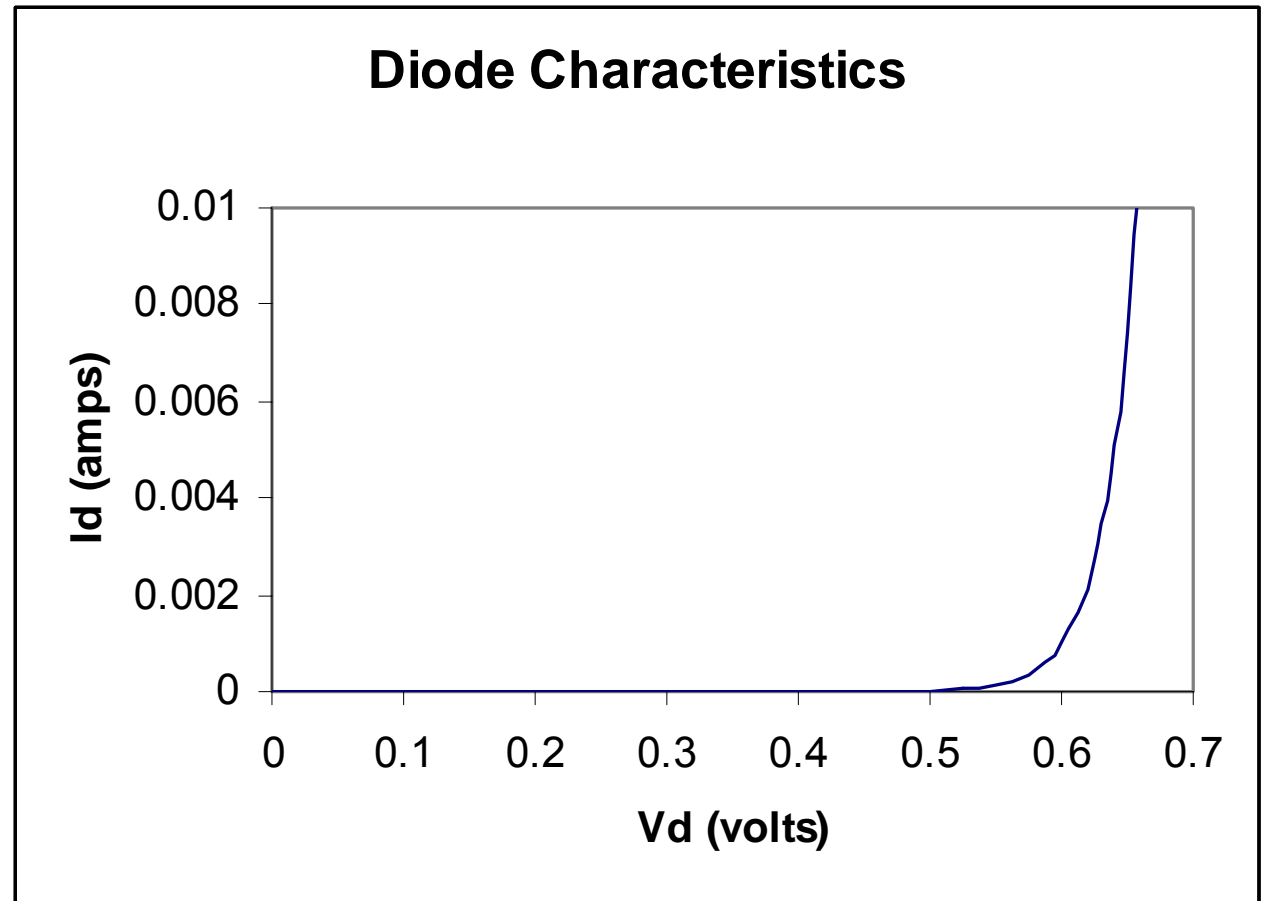
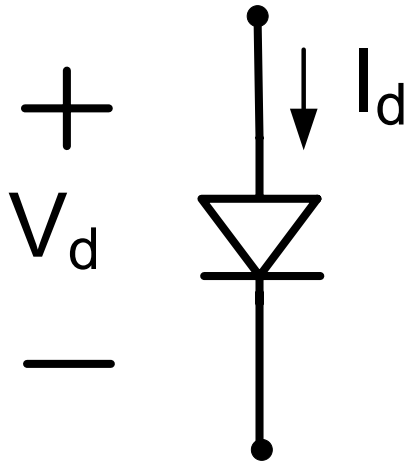
If $V_{IN} = V_M \sin \omega t$



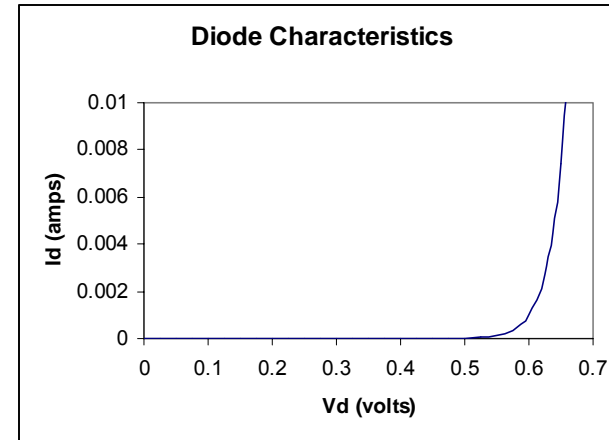
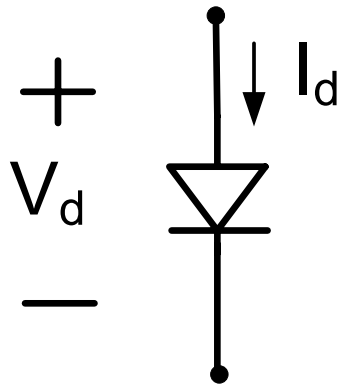
Serves as a rectifier – very useful function !

I-V characteristics of pn junction

(signal or rectifier diode)



I-V characteristics of pn junction (signal or rectifier diode)



$$I_D = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

I_S is a constant (typically $10\text{fA} < I_S < 100\text{fA}$)

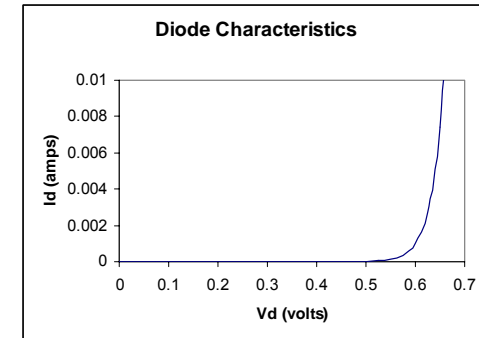
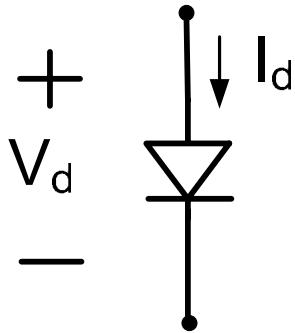
$V_t = kT/q$ k Boltzman's Constant, q charge of electron, T temp in K

$k/q = 8.63\text{E-}5 \text{ V/ } ^\circ\text{K}$

At room temperature, V_t is approximately 25mV

I_D highly temperature dependent (widely used in temp sensors!)

I-V characteristics of pn junction (signal or rectifier diode)



Termed Diode Equation

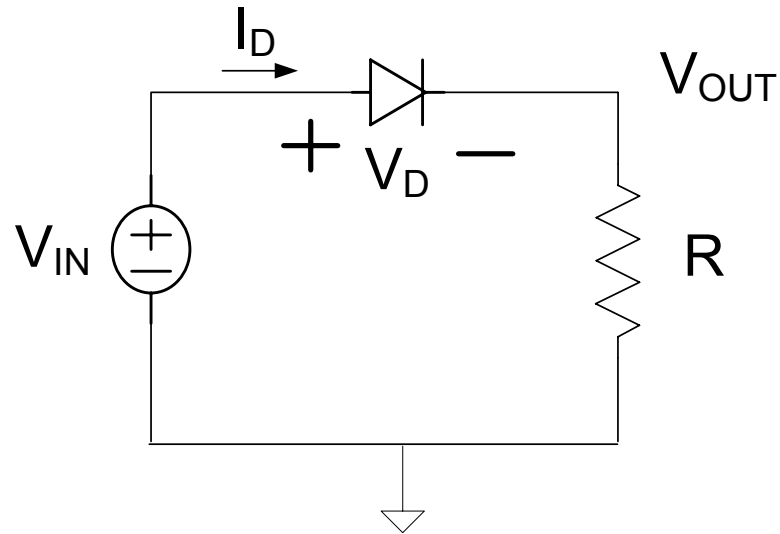
$$I_D = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

Under reverse bias, $I_D \approx -I_S$

Under forward bias, $I_D = I_S e^{\frac{V_d}{V_t}}$

Diode Equation or forward bias simplification is unwieldy to work with analytically

Consider again the basic rectifier circuit



$$V_{IN} = V_D + I_D R$$

$$V_{OUT} = I_D R$$

$$I_D = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

$$V_{OUT} = I_S R \left(e^{\frac{V_{IN} - V_{OUT}}{V_t}} - 1 \right)$$

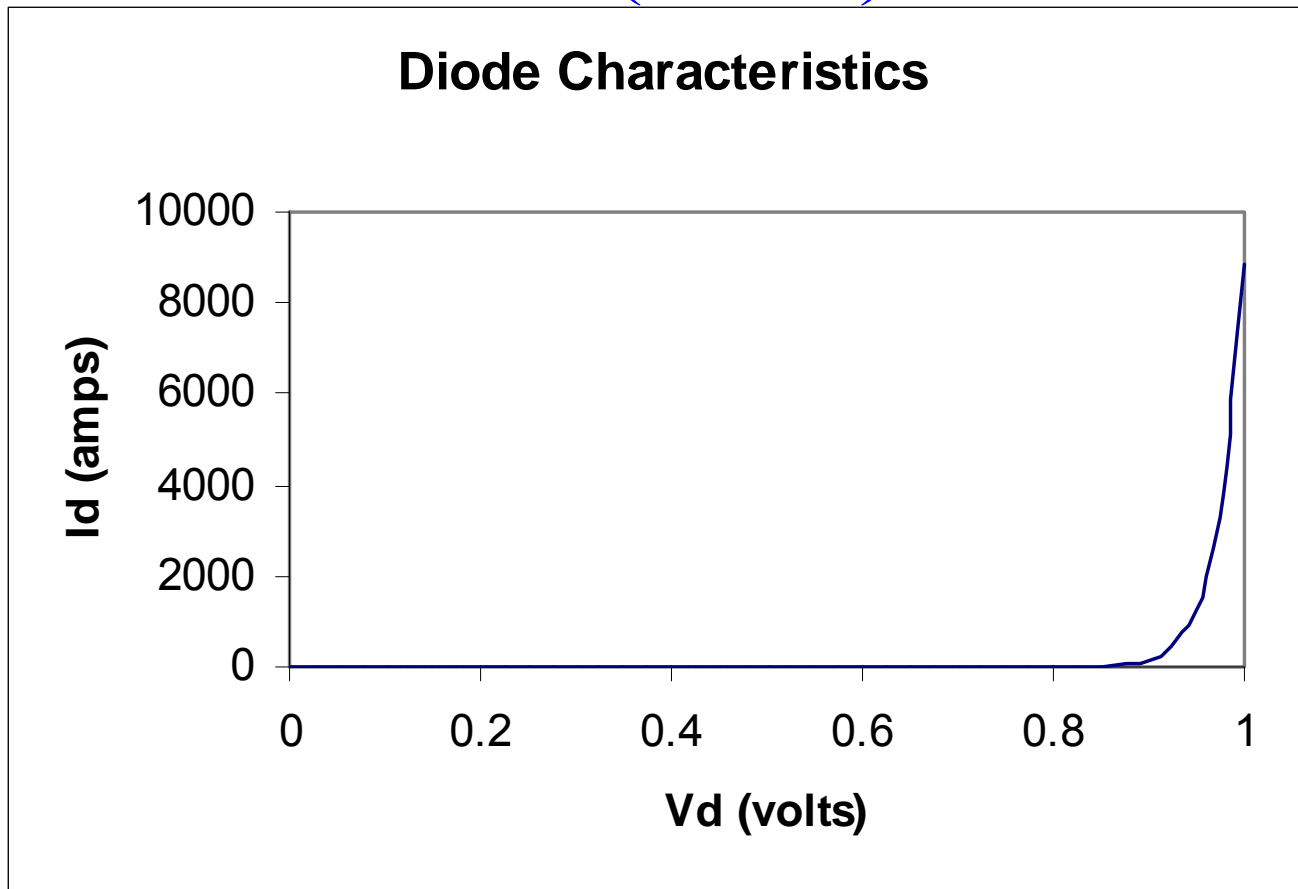
Even the simplest diode circuit does not have a closed-form solution when diode equation is used to model the diode !!

Due to the nonlinear nature of the diode equation

Simplifications are essential if analytical results are to be obtained

Lets study the diode equation a little further

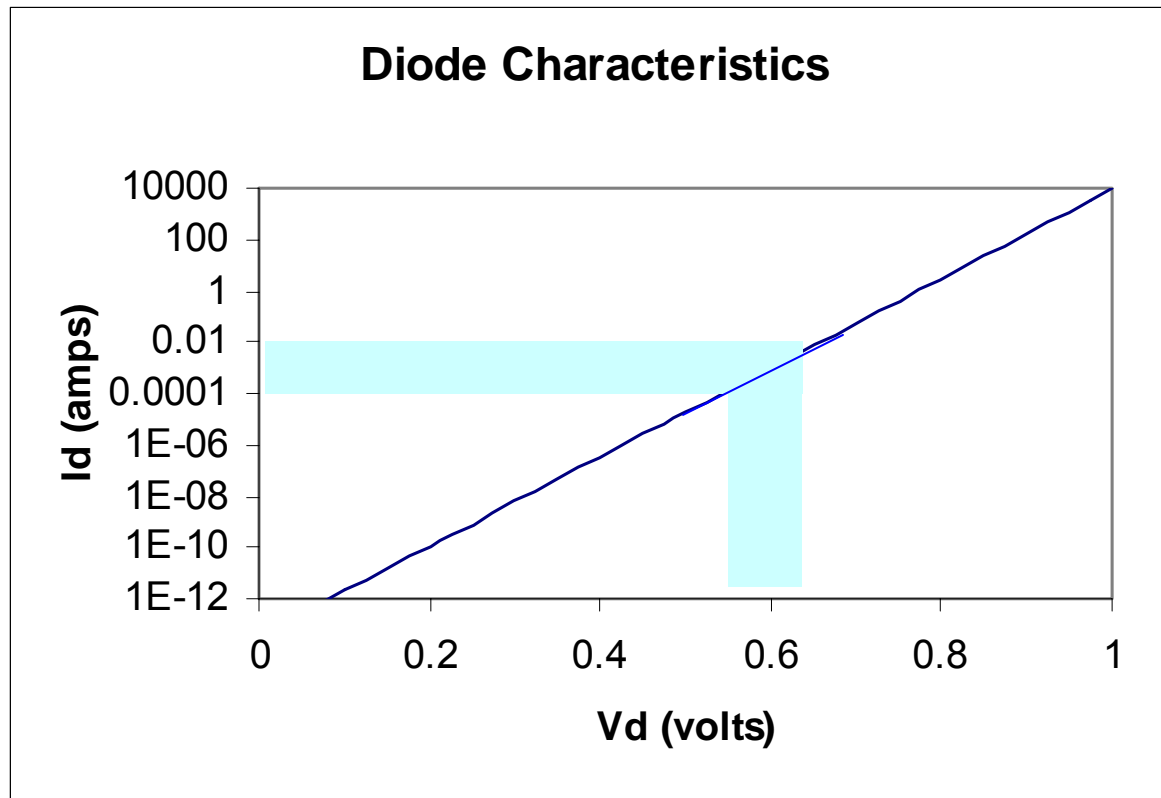
$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



Power Dissipation Becomes Destructive if $V_d > 0.85V$ (actually less)

Lets study the diode equation a little further

$$I_d = I_s \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

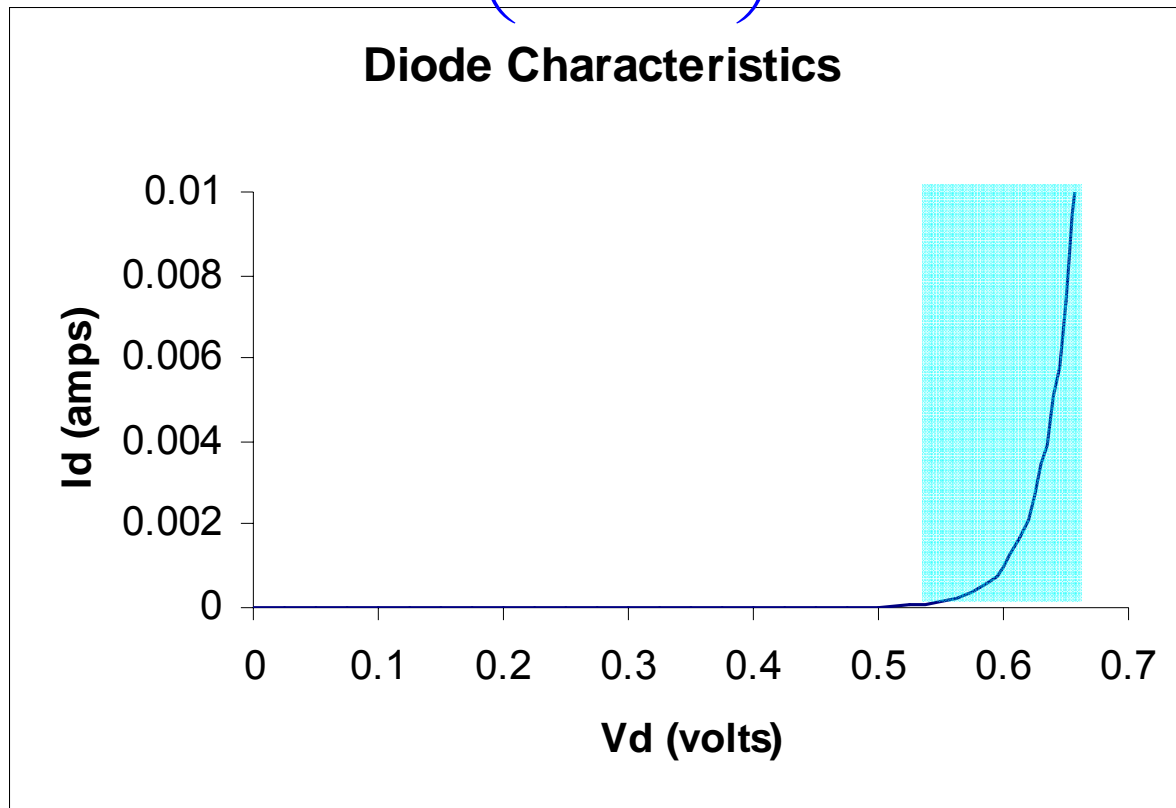


For two decades of current change, Vd is close to 0.6V

This is the most useful current range for many applications

Lets study the diode equation a little further

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

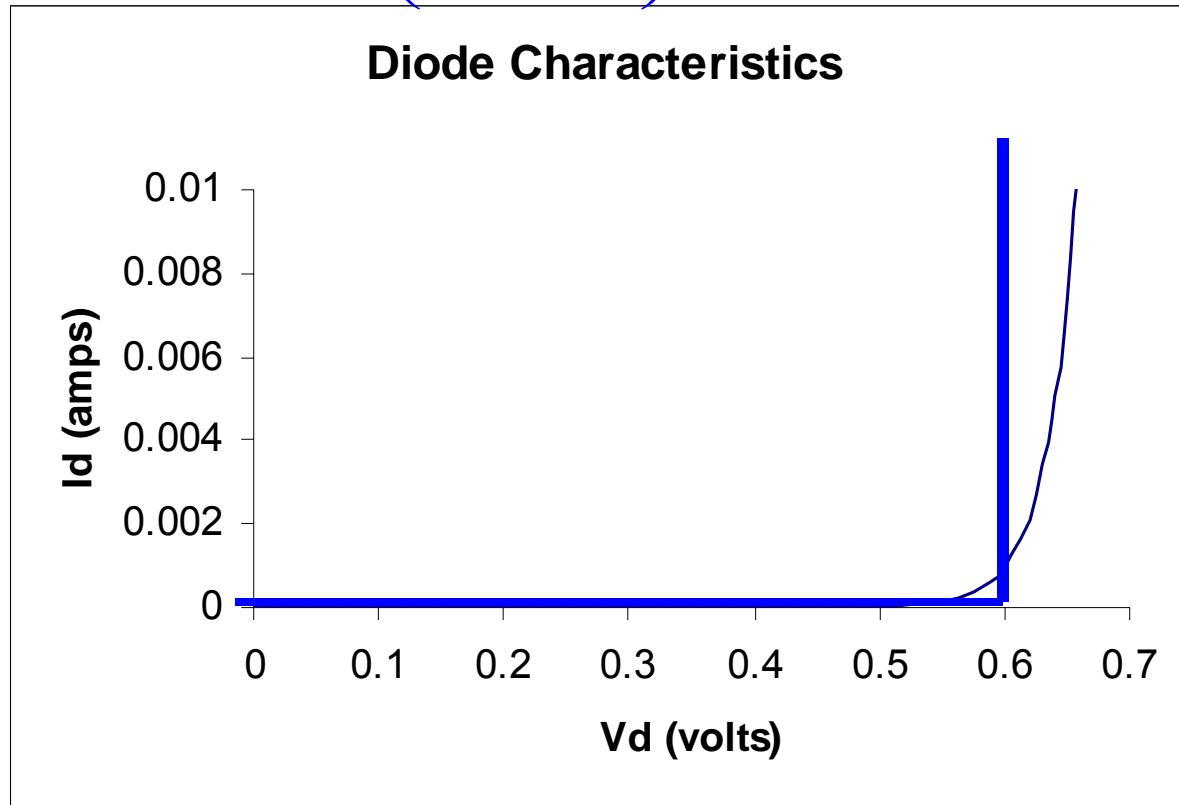


For two decades of current change, V_d is close to 0.6V

This is the most useful current range for many applications

Lets study the diode equation a little further

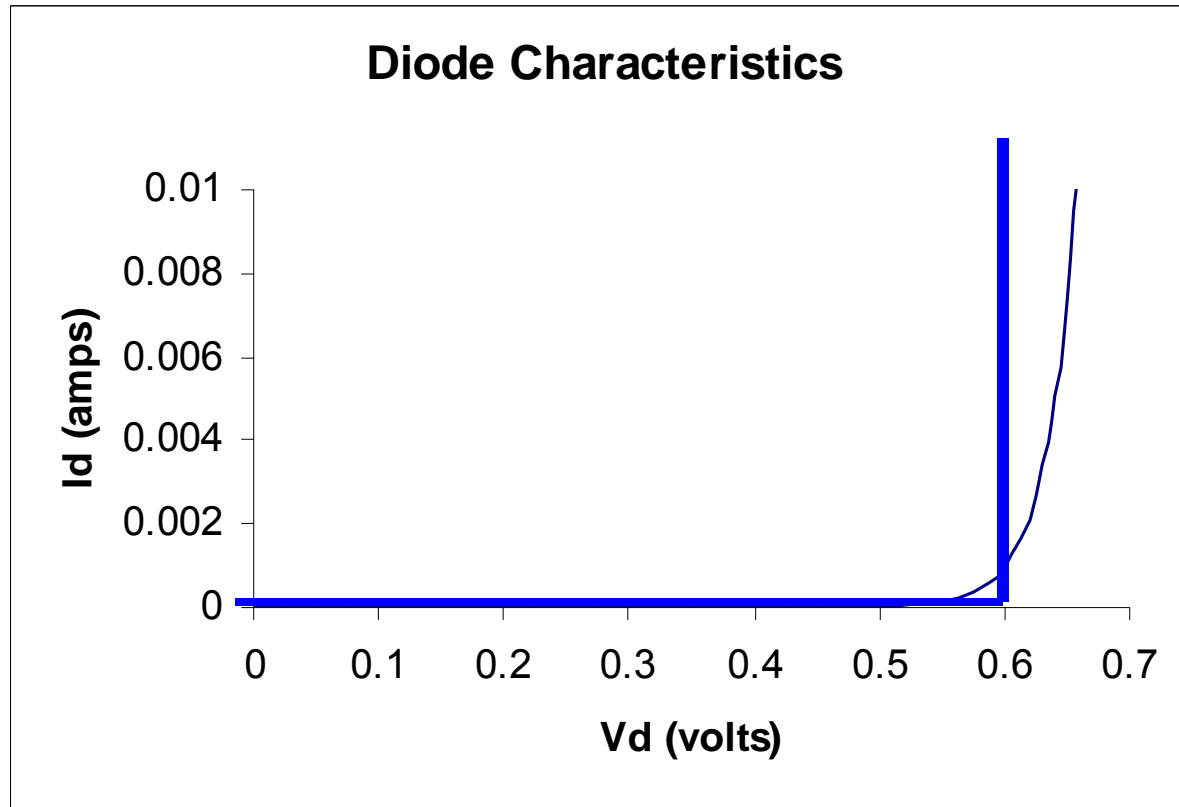
$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



Widely Used Piecewise Linear Model

Lets study the diode equation a little further

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V \quad I_d > 0$$

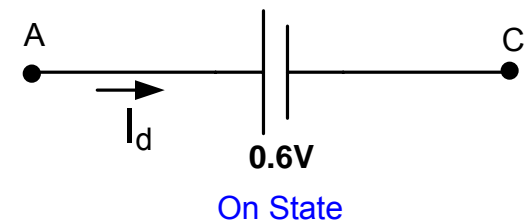
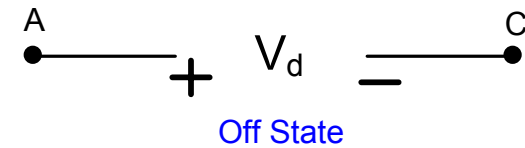
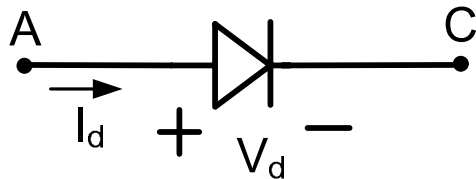
Lets study the diode equation a little further

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

Piecewise Linear Model

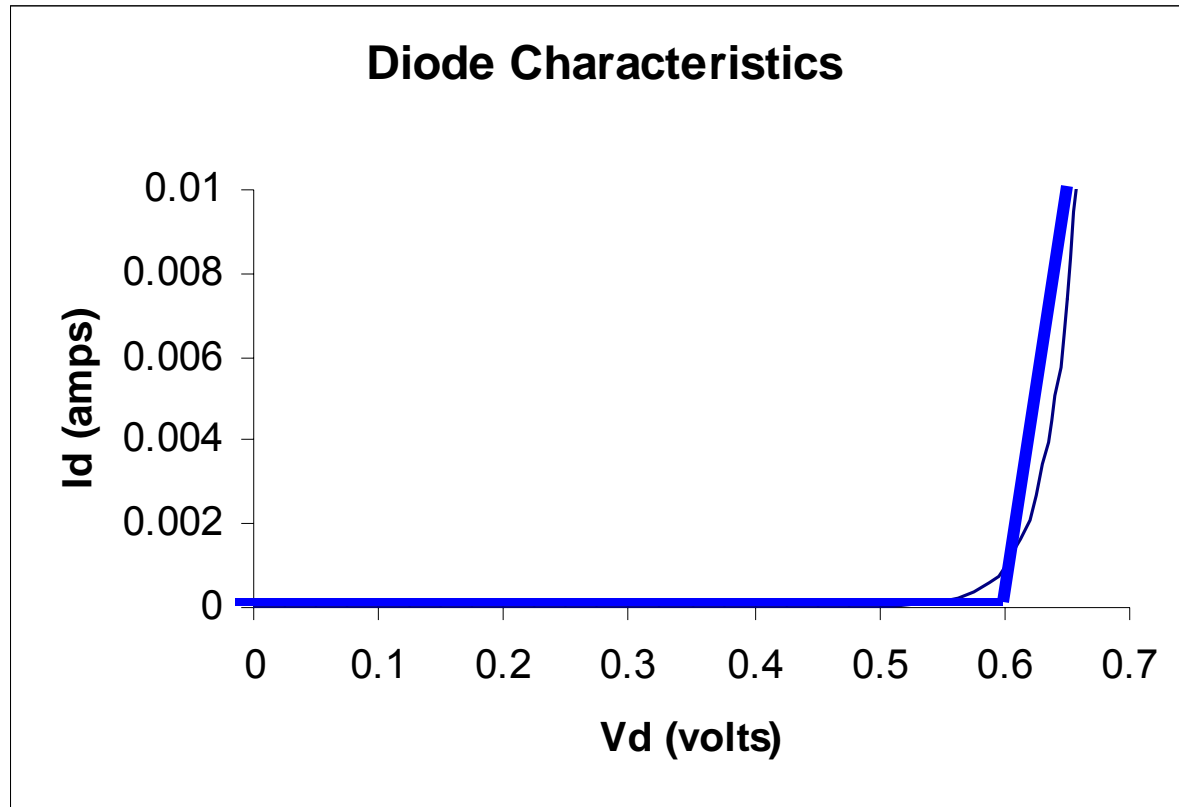
$$I_d = 0 \quad V_d < 0.6V$$
$$V_d = 0.6V \quad I_d > 0$$

Equivalent Circuit



Lets study the diode equation a little further

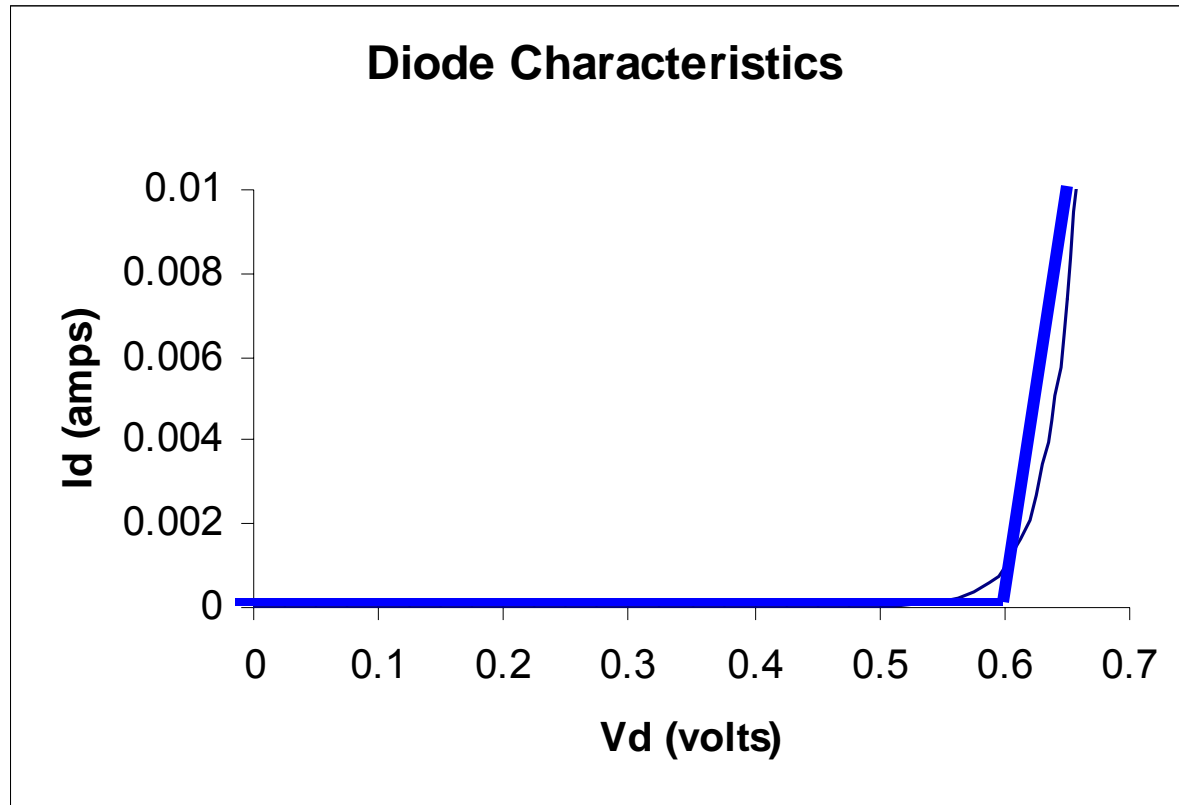
$$I_d = I_s \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



Slightly More Accurate Piecewise Linear Model

Lets study the diode equation a little further

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V + I_d R_d \quad I_d > 0$$

Lets study the diode equation a little further

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

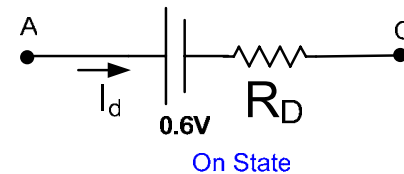
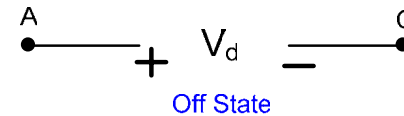
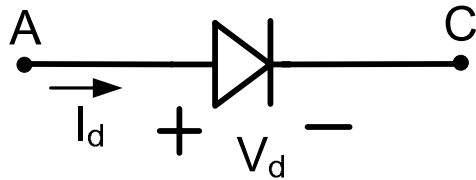
Piecewise Linear Model with Diode Resistance

$$I_d = 0 \quad V_d < 0.6V$$

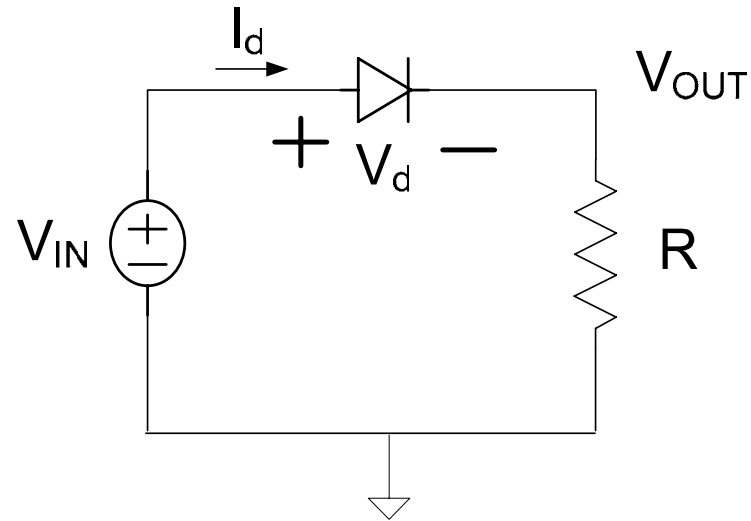
$$V_d = 0.6V + I_d R_D \quad I_d > 0$$

(R_D is rather small: often in the 20Ω to 100Ω range):

Equivalent Circuit



Consider again the basic rectifier circuit



Analyze with piecewise linear model $I_d = 0$ $V_d \leq 0.6V$

$V_d = 0.6V$ $I_d > 0$

Case 1 $I_d = 0$

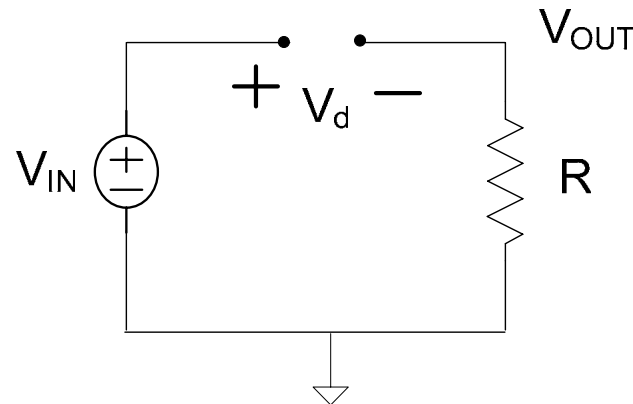
$$V_{OUT} = 0$$

valid for $V_d \leq 0.6V$

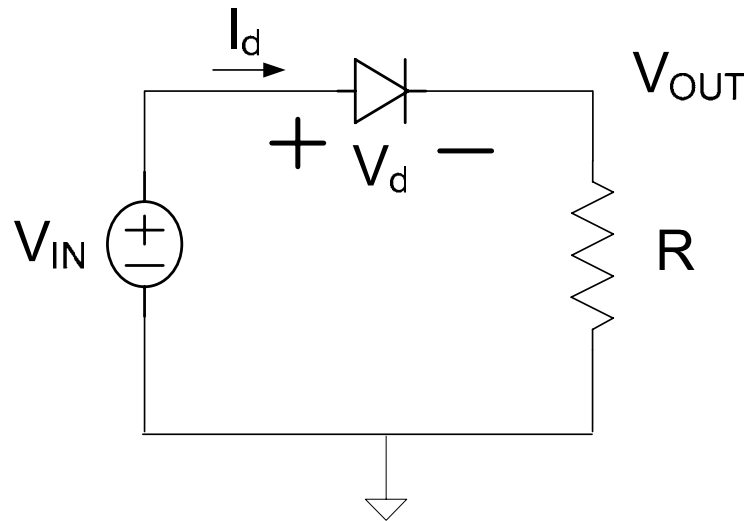
but $V_d = V_{IN}$

\therefore valid for

$$V_{IN} \leq 0.6V$$



Consider again the basic rectifier circuit



Analyze with piecewise linear model

$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V \quad I_d > 0$$

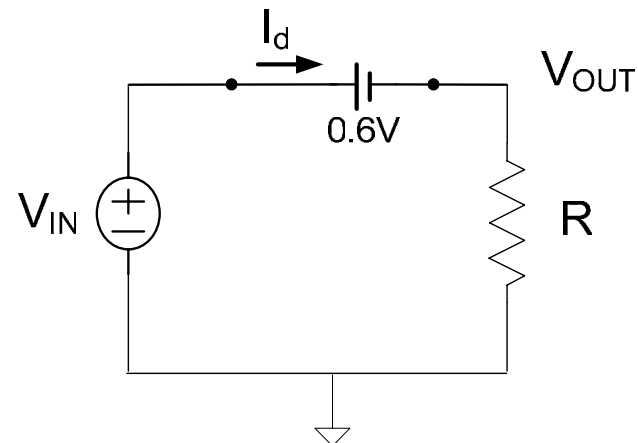
Case 2 $V_d = 0.6V$

$$V_{OUT} = V_{IN} - 0.6V$$

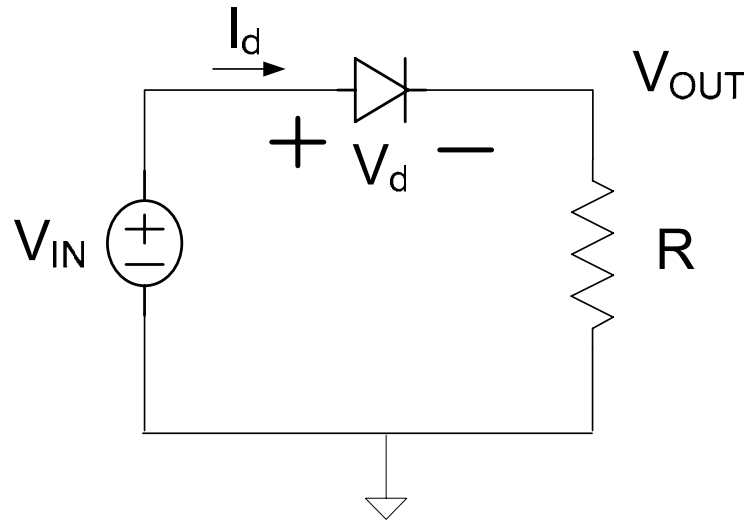
valid for $I_d > 0$

but $I_d = \frac{V_{IN} - 0.6V}{R}$

\therefore valid for $V_{IN} > 0.6V$



Consider again the basic rectifier circuit



Analyze with piecewise linear model

$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V \quad I_d > 0$$

Solution summary:

$$V_{OUT} = \begin{cases} 0 & V_{IN} \leq 0.6V \\ V_{IN} - 0.6V & V_{IN} > 0.6V \end{cases}$$

